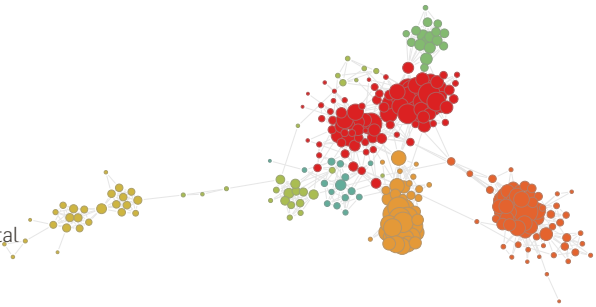


# THE TOPOLOGICAL EVOLUTION OF ONLINE SOCIAL NETWORKS

February 4, 2014  
iSocial Meeting  
Stockholm

Kaj Kolja Kleineberg  
Marián Boguñá

Departament de Física Fonamental  
Universitat de Barcelona



# AGENDA

1. Motivation & introduction
2. Empirical study
3. Basic model
4. Extended model
5. Summary & discussion

# MOTIVATION & INTRODUCTION

# DECENTRALIZED ONLINE SOCIAL NETWORKS

» The vision of a **decentralized** Ubiquitous Social Networking Layer in the **absence of central management and control.**«<sup>1</sup>

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<sup>1</sup><http://isocial-itn.eu>



# DECENTRALIZATION IN MONETARY SECTOR



## THE BENEFIT FROM MODELS

- Overlay Infrastructure for Decentralized Online Social Networking Services
- Data storage & distribution
- Security, privacy & trust
- **Modelling** and Simulation



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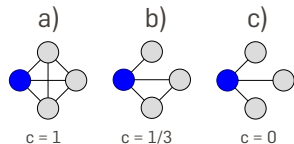


- 
- **Quantitative** models can identify **mechanisms** for:
    - + Evolution of **topological structure** of the network
    - + **Competition** between different online social networks



## BRIEF INTRODUCTION

- **Local clustering coefficient:**  $c_i$  number of connected pairs of neighbors divided by total number of pairs of neighbors
- **Mean local clustering:** average of  $c_i$
- **Giant connected component (GCC):** Size of the largest subgraph of a network in which each pair of nodes is connected by a path.
- **Average shortest path length:** Average shortest distance ( $d_{ij}$ ) between each pair of nodes in the GCC.
- **Network diameter:** The network diameter (within the GCC) is defined as the maximum of  $d_{ij}$



$$l = \max_{ij} \{d_{ij}\} .$$

# EMPIRICAL STUDY

## CASE STUDY: »POKEC«

**Pokec** kolja čo je nové rýchla pošta email priatelia PLUS odhlásiť miestnosti používatelia stretko

**kolja** PLUS O MNE NÁSTENKA FOTKY VIDEÁ

Muž, 28 rokov, Zahraničie - ostatné  
Na Pokeni od dnes  
● prihlásený

[upraviť profil](#) [zmeniť vzhľad](#) [Iné](#)

” Doteraz si nič nenapísal.

**Životný štýl**

Moje záľuby ..... sports, travel, watching movies, party, sleep, friends, listening to music

Dobré jedlo si vychutnám .... in bed

Domáce zvieratá ..... spider, parrot

**Komentáre** (0)

kolja práve píšeš... [Pridať komentár](#)

**Komentuj**

# POKEC SLOVAKIAN ONLINE SOCIAL NETWORK

Slovakia

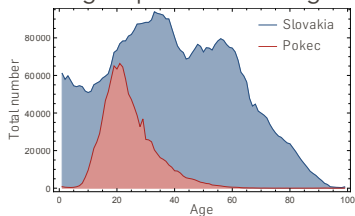
Population  
5,410,836



Pokec empirical network

Users  
1,632,803

Age-specific coverage





# POKEC SLOVAKIAN ONLINE SOCIAL NETWORK

## Slovakia

Population  
5,410,836



## Pokec empirical network

Users  
1,632,803

- ▶ Isolated network
- ▶ Very high population coverage
- ▶ Evolution 1999-2012
- ▶ 1.2 million nodes in bi-directional subgraph

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## Pokec empirical network

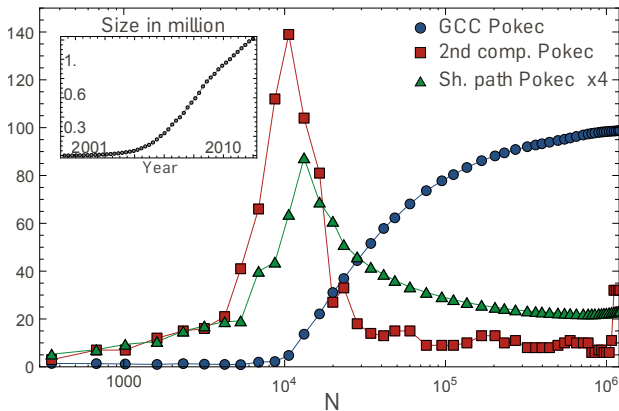
Users  
1,632,803

- ▶ Isolated network
- ▶ Very high population coverage
- ▶ Evolution 1999-2012
- ▶ 1.2 million nodes in bi-directional subgraph

Network is **isolated**, **active** & contains a **large fraction** of a priori susceptible individuals.

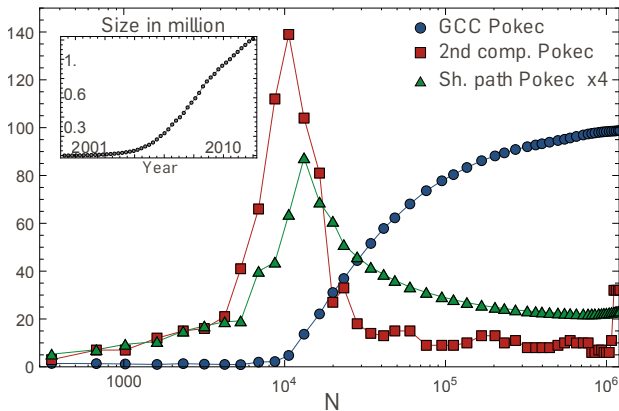
## PHASE TRANSITION

## Evolution of Pokec network



## PHASE TRANSITION

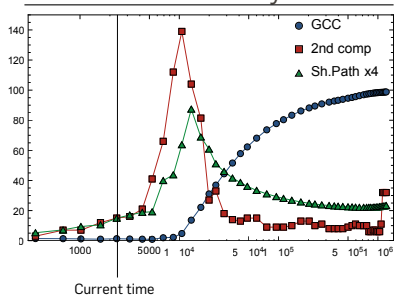
## Evolution of Pokec network



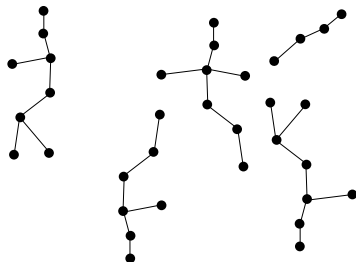
Network exhibits **dynamical phase transition**  
between **disconnected** and **connected** phase.

## STRUCTURE

## Connectivity

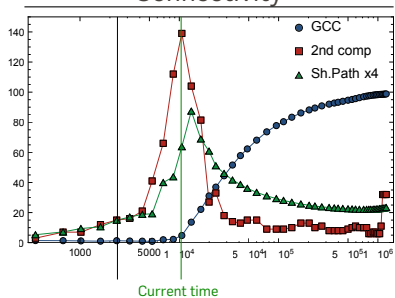


## Structure

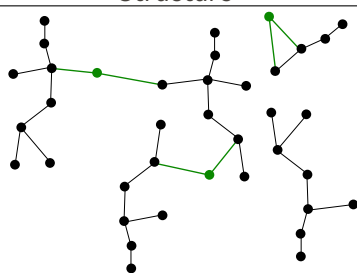


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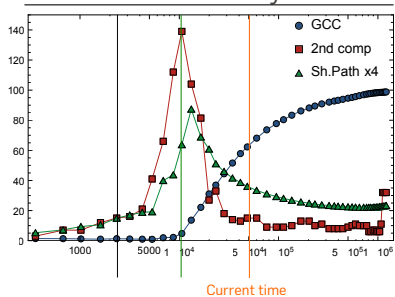


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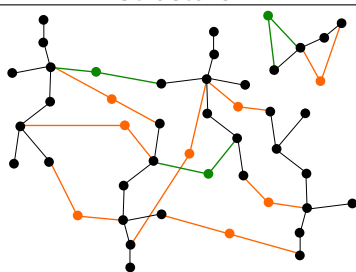


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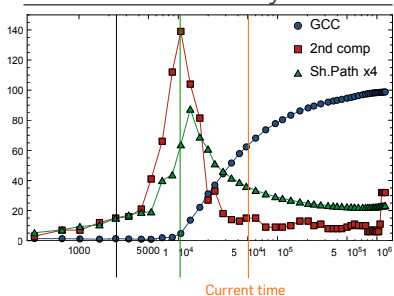


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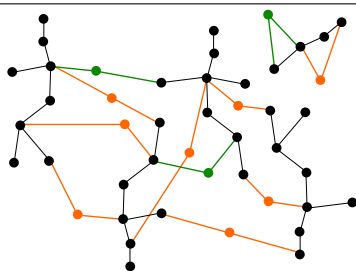


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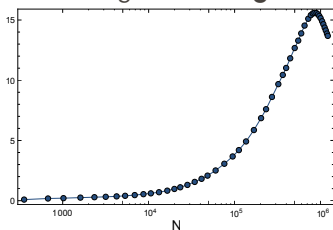


Multiple components grow to **chain-like** structures until they become **connected** and form **shortcuts**.

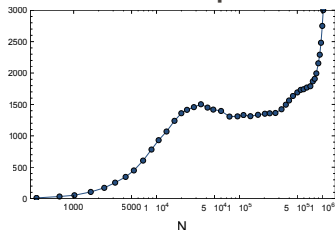


# TOPOLOGICAL EVOLUTION OF POKEC

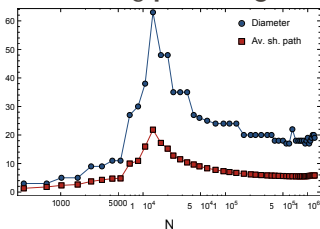
## Growing mean degree



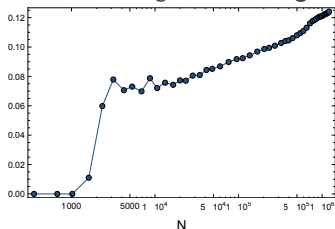
## Number of components



## Shrinking pathlength



## Increasing clustering

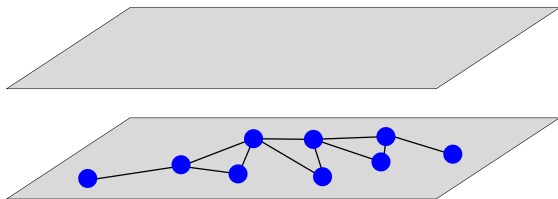


## SUMMARY: EMPIRICAL STUDY

- Study evolution of **large, active & isolated** online social network
- Dynamical **phase transition** from disconnected to connected
- **Shrinking** diameter & pathlength
- **Increasing** clustering coefficient

# BASIC MODEL

## TWO-LAYER DESIGN: THE SOCIAL BACKBONE



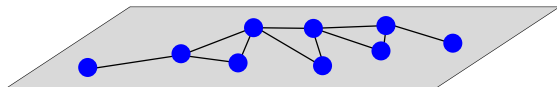
Online social  
network layer

Traditional contact  
network layer

## TWO-LAYER DESIGN: THE SOCIAL BACKBONE



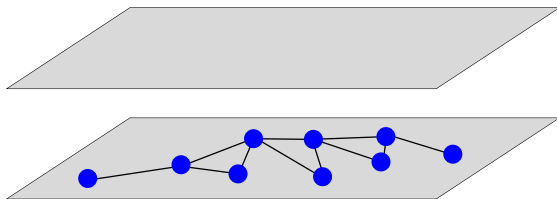
Online social network layer



Traditional contact network layer

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- ▶ Underlying subgraph of **a priori susceptible** nodes from **aggregation** of all contact networks except OSN

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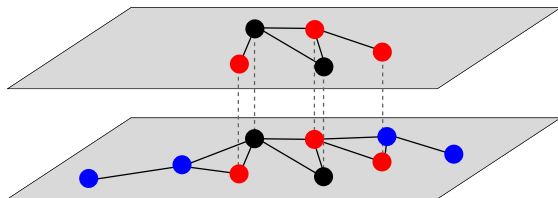


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- ▶ Underlying subgraph of **a priori susceptible** nodes from **aggregation** of all contact networks except OSN
- ▶ Start with **empty online social network** layer

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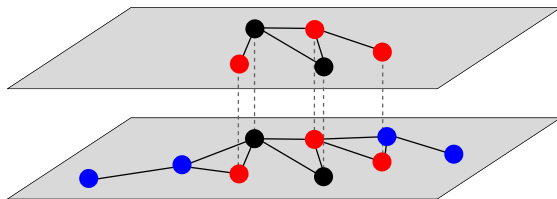


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**Question:** What do we use as **underlying contact network** layer?



# UNDERLYING NETWORK: THE VALIDATION CONCEPT

## Synthetic network

For instance  
S1-model

Control of degrees,  
clustering and sizes



Model validation



## Empiric network

Final snapshot of  
empiric network

Control of degrees,  
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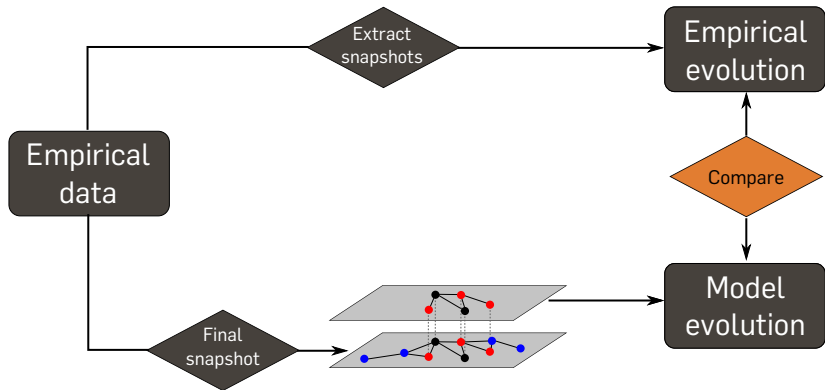
Control of degrees,  
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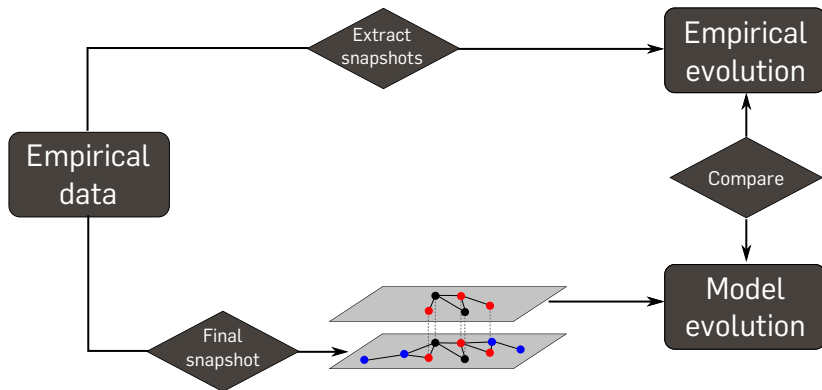
Model validation 

Only **empiric network** as underlying layer allows  
**rigorous validation** of the model.

# UNDERLYING NETWORK: THE VALIDATION CONCEPT



## UNDERLYING NETWORK: THE VALIDATION CONCEPT



**Question:** Which are the **mechanisms** that determine subscriptions and allow to **reproduce the evolution**?

# VIRALITY AND MASS MEDIA INFLUENCE

## Mass media

---

»Sources of information that reach and **influence large numbers** of people.«

**Model:** Random subscriptions (affects everybody equally).

**Impact:** Creates many disconnected components.

## Virality

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»The tendency of information to be circulated rapidly and widely **from one to another**.«

**Model:** Like the spread of a virus in SIS model.

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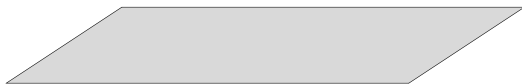
**Virality** and **mass media** effect play **complementary roles** for the evolution of the network topology.

# MODEL MECHANISM

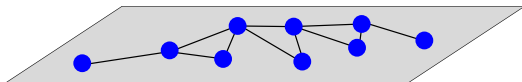
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Online social  
network layer



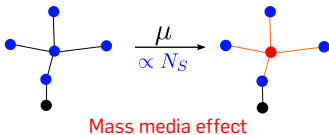
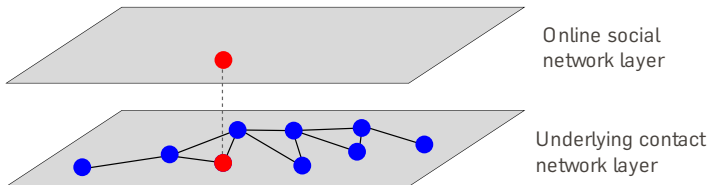
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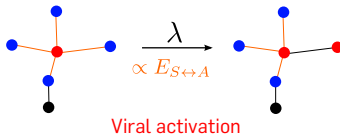
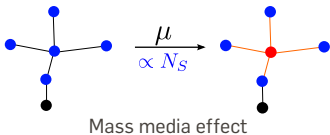
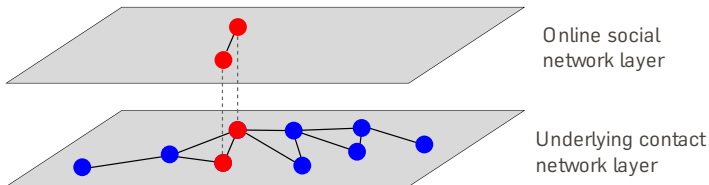


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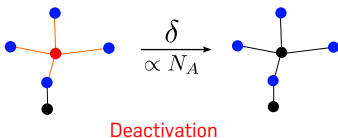
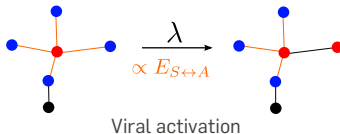
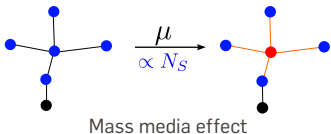
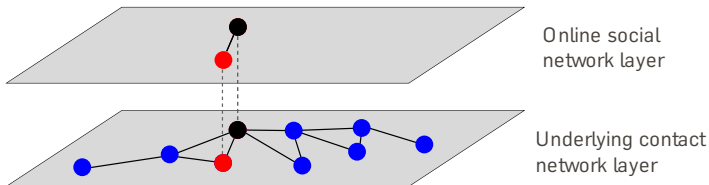


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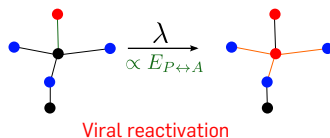
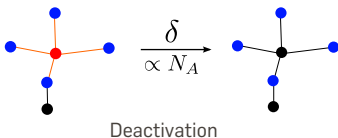
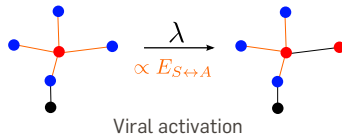
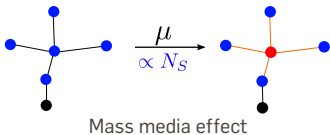
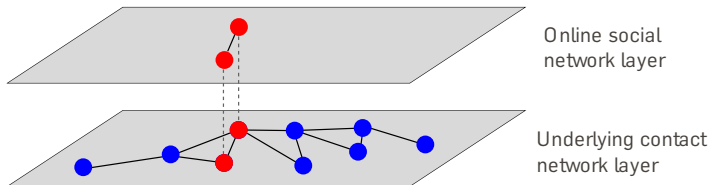


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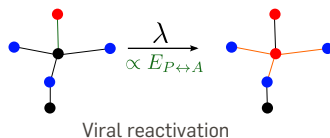
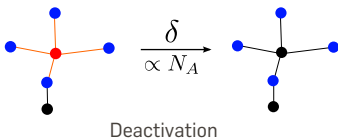
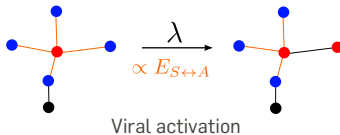
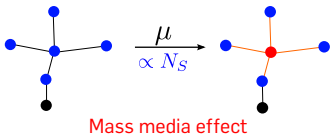
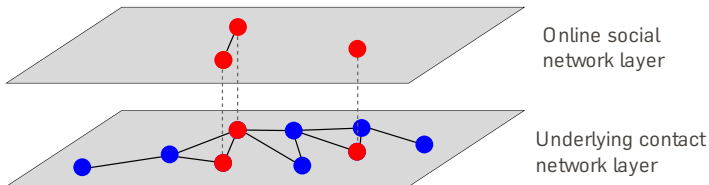


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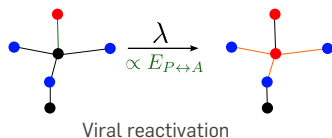
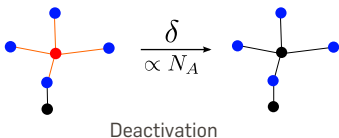
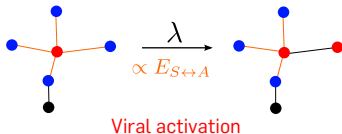
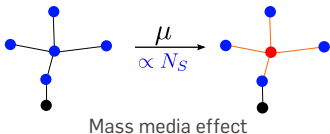
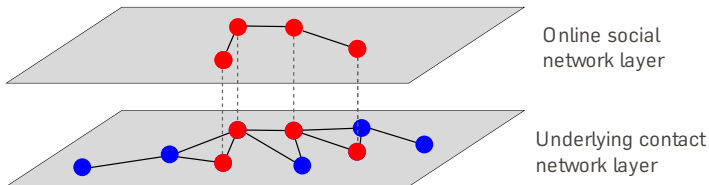


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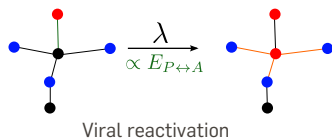
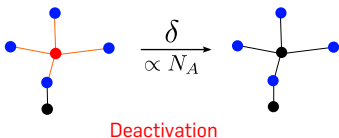
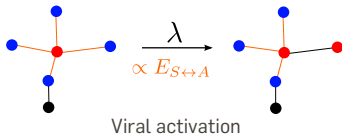
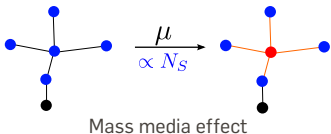
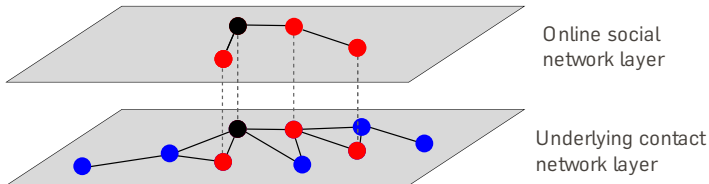


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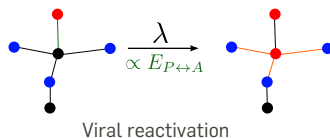
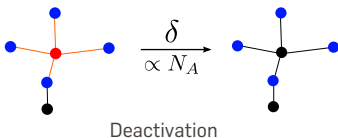
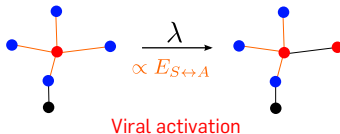
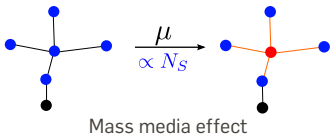
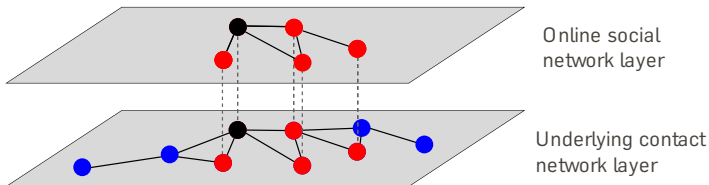


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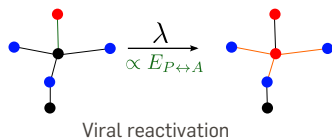
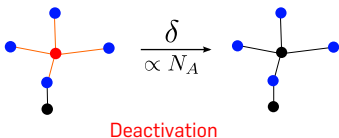
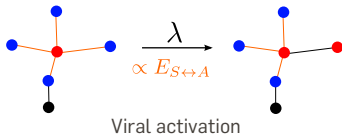
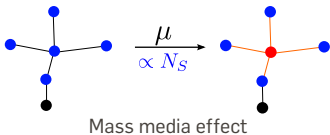
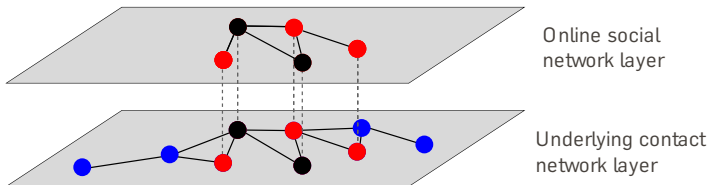


# MODEL MECHANISM

S: Susceptible ●  
only offline  
can be activated

P: Passive ●  
online and offline  
do not activate

A: Active ●  
online and offline  
do activate



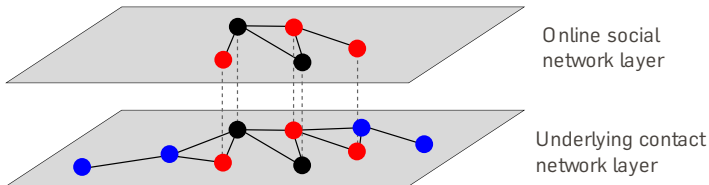


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Mass media effect

Deactivation

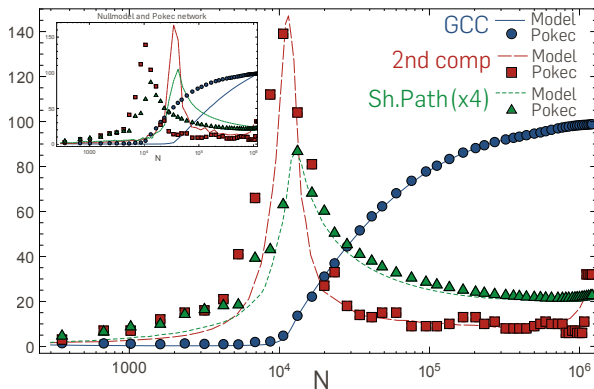
Viral activation

Viral reactivation

Can we **reproduce the empirical evolution** with **viral** and **mass media** dynamics?

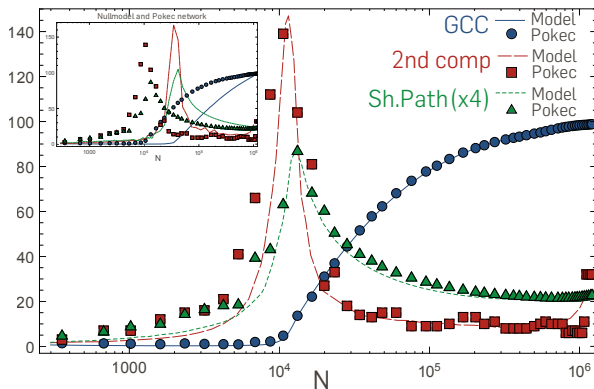
# RESULTS FROM VIRALITY MASS MEDIA MODEL

Basic model and empiric network



## RESULTS FROM VIRALITY MASS MEDIA MODEL

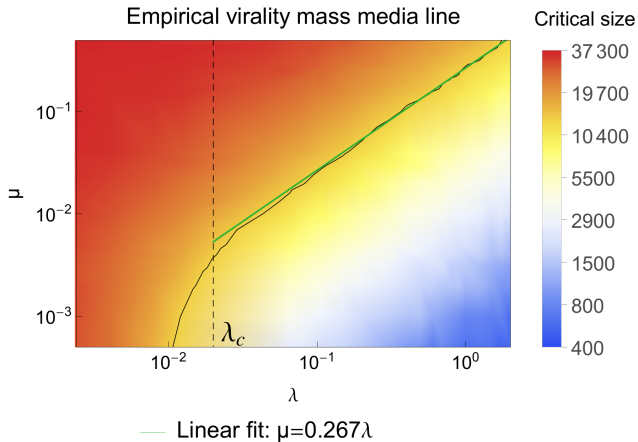
Basic model and empiric network



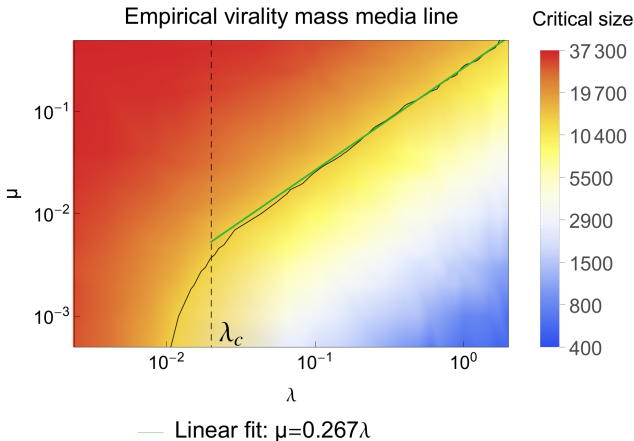
**Interplay** between **virality** and **mass media** dynamics is the underlying principle of the OSN evolution.

## RESULTS FROM VIRALITY MASS MEDIA MODEL

# BALANCE BETWEEN VIRALITY AND MASS MEDIA INFLUENCE



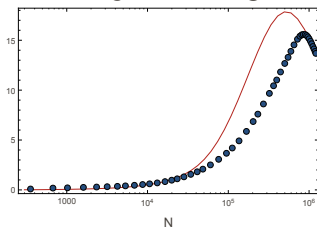
# BALANCE BETWEEN VIRALITY AND MASS MEDIA INFLUENCE



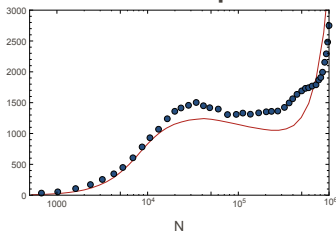
**Virality** is **four times** stronger than the **mass media** effect.

# TOPOLOGICAL EVOLUTION

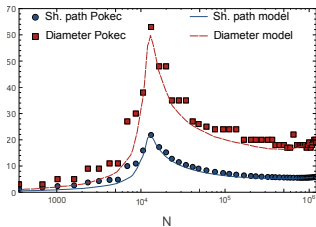
## Growing mean degree



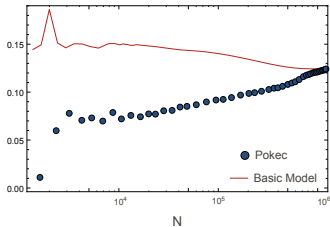
## Number of components



## Shrinking pathlength



## Decreasing clustering



## SUMMARY: VIRALITY MASS MEDIA MODEL

- **Social structure** underlying the OSN matters
- **Mechanisms: Virality** and **mass media** influence
- **Quantification** of **viral** and **mass media** effect
- Global topology ✓
- Local topology ✗



# EXTENDED MODEL

# LOCAL NEIGHBORHOOD STRUCTURE

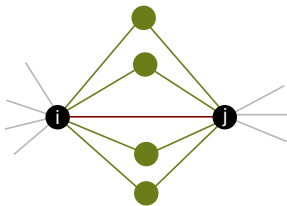
»It is argued that the degree of **overlap of two individuals' friendship networks** varies directly with the **strength of their tie** to one another.«<sup>1</sup>

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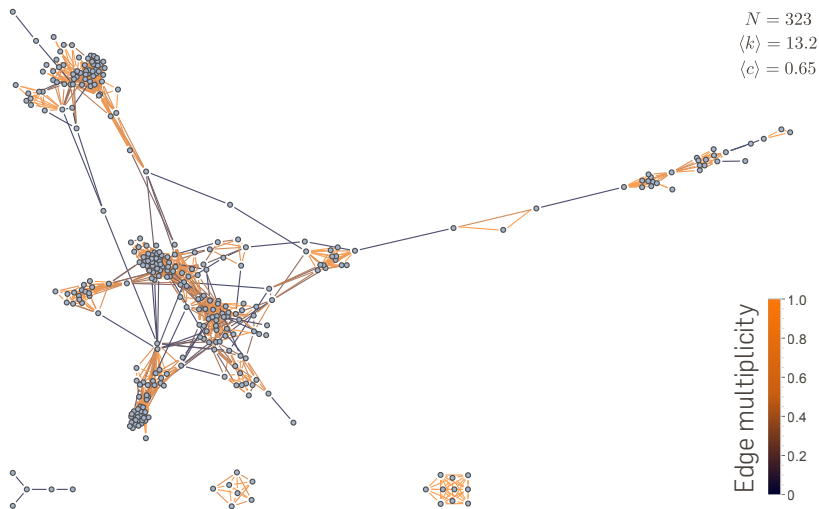
**Edge multiplicity** is given by the number of the **common neighbors** of the nodes at the end of the edge.

$$m_{ij} = \frac{N[\blacksquare]}{\min[k_i, k_j]}$$

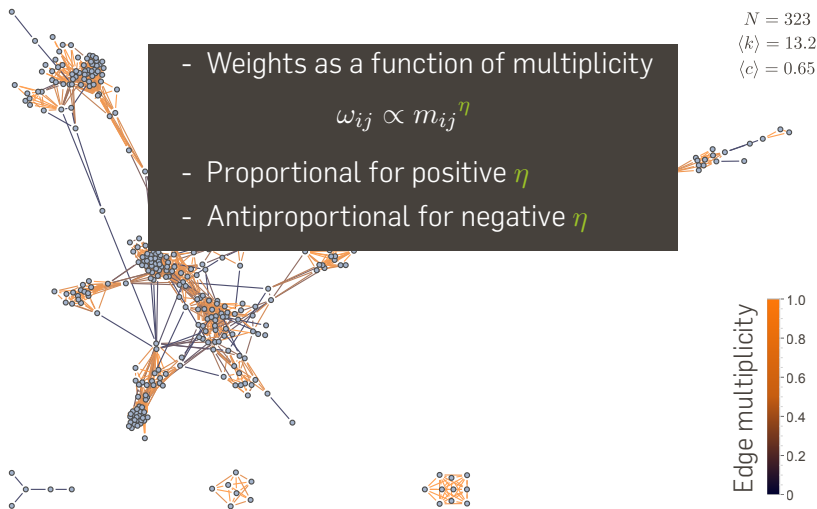
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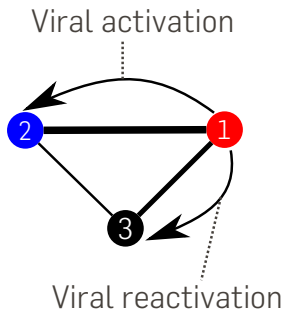
## MULTIPLICITY AND LINK WEIGHTS



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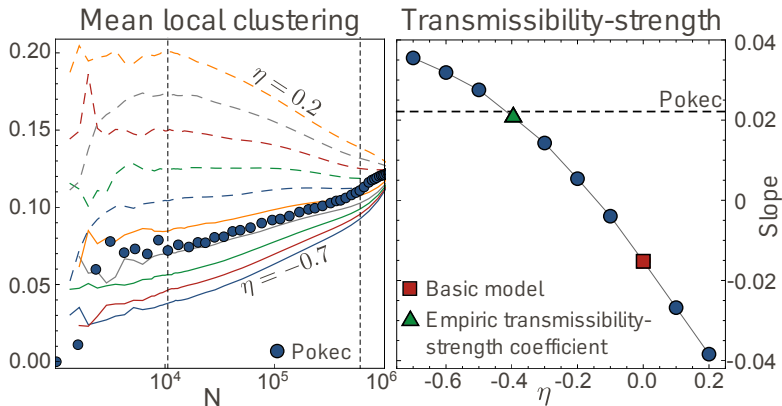


## LOCAL TRANSMISSIBILITY OF THE VIRAL EFFECT

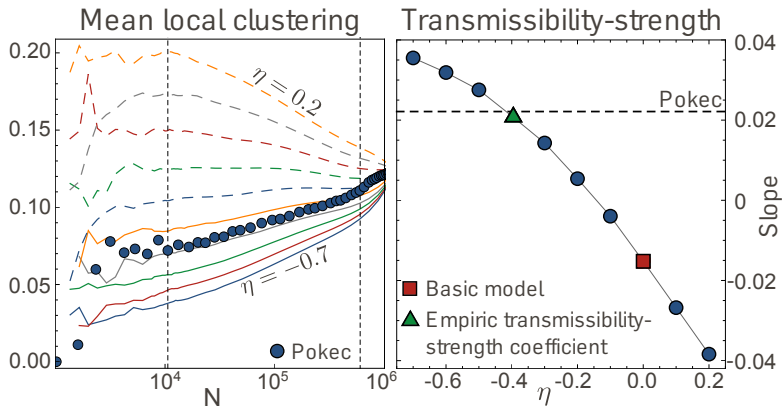


- **Viral activation** ( $1 \leftrightarrow 2$ ) occurs with **rate**  $\lambda\omega_{1,2}$
- **Viral reactivation** ( $1 \leftrightarrow 3$ ) occurs with **rate**  $\lambda\omega_{1,3}$
- **Mass media** effect and **de-activation** are not affected by assigned weights

## TRANSMISSIBILITY AND SOCIAL TIES



## TRANSMISSIBILITY AND SOCIAL TIES

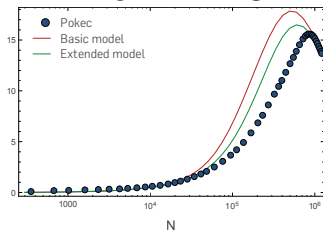


**Weak ties** exhibit a higher transmissibility for the **viral effect** than strong ties.

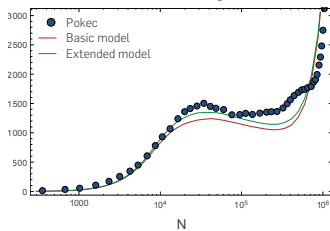


## COMPARISON BASIC &amp; EXTENDED MODEL

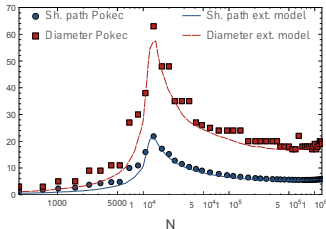
## Growing mean degree



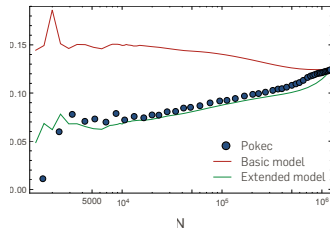
## Number of components



## Shrinking pathlength



## Increasing clustering



## SUMMARY: EXTENDED VIRALITY MASS MEDIA MODEL

- **Strength** of ties function of **multiplicity**
- **Viral** effect favors **weak ties**
- Global topology ✓
- Local topology ✓

# SUMMARY & DISCUSSION

## SUMMARY: TAKE HOME MESSAGES

- We need **models** to understand the underlying **mechanisms**
- **Validation concept:** Reproduction of empirical evolution
- **Two-layer** model: **Identify & quantify virality** and **mass media** influence as underlying **mechanisms**
- Local topological evolution: **higher viral transmissibility** for **weak ties**

## OUTLOOK & FURTHER RESEARCH

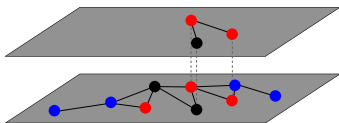


Figure: Single OSN layer.

## OUTLOOK & FURTHER RESEARCH

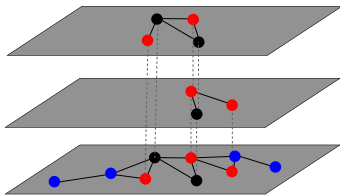


Figure: Multiple OSN layers.

# OUTLOOK & FURTHER RESEARCH

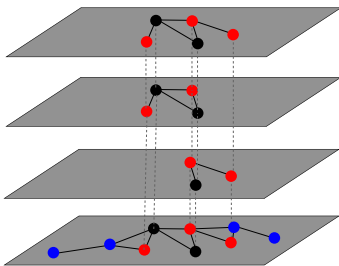


Figure: Multiple OSN layers.

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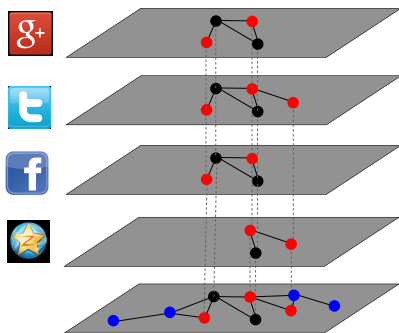


Figure: Multiple OSN layers.

**Multiple OSN layers:**

- Competition
- Parameters  $\vec{\lambda}, \vec{\mu}$
- For instance:

$$\vec{\lambda} = \vec{\lambda}(\vec{A}, \vec{P}, \vec{S})$$

$$\vec{\mu} = \vec{\mu}(\vec{A}, \vec{P}, \vec{S})$$

- Distribution of network sizes, activities etc...



## OUTLOOK &amp; FURTHER RESEARCH

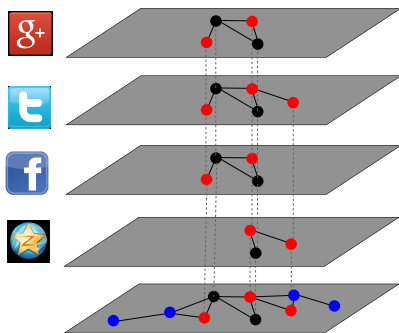


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- Distribution of network sizes, activities etc...

**Ongoing research:** Can we reproduce the distribution of empiric OSN sizes with a **competition model**?

## QUESTIONES, COMMENTS & MORE



L. Takac and M. Zabovsky.

»Data analysis in public social networks.«

*International Scientific Conference and International Workshop Present  
Day Trends of Innovations, 2012.*



K. Kleineberg and M. Boguñá.

»Trade-off between virality and mass media influence in the topological  
evolution of online social networks«.

*In progress.*

Please don't hesitate to contact me.

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kkl@correu.ffn.ub.edu

